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## METHOD AND APPARATUS FOR SOLVING AN UNCONSTRAINED GLOBAL OPTIMIZATION PROBLEM

## **ABSTRACT**

One embodiment of the present invention provides a system that receives a representation of the function f and stores the representation in a memory. Next, the system performs an interval global optimization process to compute guaranteed bounds on a globally minimum value of the function  $f(\mathbf{x})$  over a subbox X. This interval global optimization process applies term consistency to a set of relations associated with the function f over the subbox X, and excludes any portion of the subbox X that violates any member of the set of relations. It also applies box consistency to the set of relations associated with the function f over the subbox X, and excludes any portion of the subbox X that violates the set of relations. The interval global optimization process also performs an interval Newton step on the subbox X to produce a resulting subbox Y, wherein the point of expansion of the interval Newton step is a point x within the subbox X, and wherein performing the interval Newton step involves evaluating the gradient g(x)of the function  $f(\mathbf{x})$  using interval arithmetic. The system integrates the sub-parts of the process with branch tests designed to increase the overall speed of the process.